



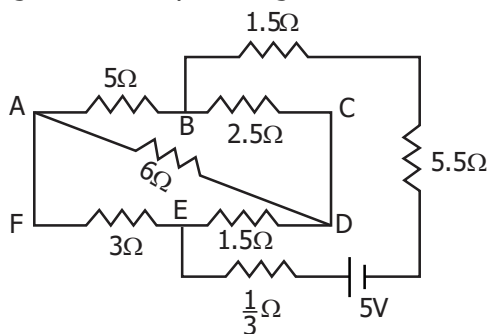
**PHYSICS**

**(Question Paper with Answer & Solution)**

**Paper Code : 47**

**Test Date : 04.05.2025**

1. The current passing through the battery in the given circuit is :



- (1) 1.5 A                      (2) 2.0 A                      (3) 0.5 A                      (4) 2.5 A

**Ans. (3) 0.5 A**

**Sol.**  $6\Omega$  will remove by Balanced Wheatstone bridge

$$R_{eq} \text{ of bridge} = \frac{8 \times 4}{12} = \frac{8}{3}$$

$$R_{eq} = \frac{8}{3} + 7 + \frac{1}{3} = 10\Omega$$

$$i = \frac{5}{10} = .5 \text{ Amp}$$

2. The electric field in a plane electromagnetic wave is given by  $E_z = 60 \cos (5x + 1.5 \times 10^9 t) \text{ V/m}$ . Then expression for the corresponding magnetic field is (here subscripts denote the direction of the field)

- (1)  $B_y = 60 \sin (5x + 1.5 \times 10^9 t) \text{ T}$                       (2)  $B_y = 2 \times 10^{-7} \cos (5x + 1.5 \times 10^9 t) \text{ T}$   
(3)  $B_x = 2 \times 10^{-7} \cos (5x + 1.5 \times 10^9 t) \text{ T}$                       (4)  $B_z = 60 \cos (5x + 1.5 \times 10^9 t) \text{ T}$

**Ans. (2)**

**Sol.**  $B = \frac{E}{C} = \frac{60}{3 \times 10^8} = 2 \times 10^{-7} \text{ T along } y$

3. A pipe open at both ends has a fundamental frequency  $f$  in air. The pipe is now dipped vertically in a water drum to half of its length. The fundamental frequency of the air column is now equal to :

- (1)  $2f$                       (2)  $\frac{f}{2}$                       (3)  $f$                       (4)  $\frac{3f}{2}$

**Ans. (3) f**

**Sol.**  $f_{\text{open pipe}} = \frac{v}{2l} = f$

$$f_{\text{closed pipe}} = \frac{v}{4l'} = \frac{v}{4 \times \frac{l}{2}} = \frac{v}{2l} = f$$



4. An electron (mass  $9 \times 10^{-31}$  kg and charge  $1.6 \times 10^{-19}$  C) moving with speed  $c/100$  ( $c$  = speed of light) is injected into a magnetic field  $\vec{B}$  of magnitude  $9 \times 10^{-4}$  T perpendicular to its direction of motion. We wish to apply an uniform electric field  $\vec{E}$  together with the magnetic field so that the electron does not deflect from its path. Then : (speed of light  $c = 3 \times 10^8$  ms $^{-1}$ )

- (1)  $\vec{E}$  is parallel to  $\vec{B}$  and its magnitude is  $27 \times 10^4$  V m $^{-1}$   
 (2)  $\vec{E}$  is perpendicular to  $\vec{B}$  and its magnitude is  $27 \times 10^4$  V m $^{-1}$   
 (3)  $\vec{E}$  is perpendicular to  $\vec{B}$  and its magnitude is  $27 \times 10^2$  V m $^{-1}$   
 (4)  $\vec{E}$  is parallel to  $\vec{B}$  and its magnitude is  $27 \times 10^2$  V m $^{-1}$

Ans. (3)  $\vec{E}$  is perpendicular to  $\vec{B}$  and its magnitude is  $27 \times 10^2$  V m $^{-1}$

Sol.  $V = \frac{E}{B}$

$$E = \frac{c}{100} \cdot B = \frac{3 \times 10^8}{100} \times 9 \times 10^{-4}$$

$$= 27 \times 10^2 \text{ V/m.}$$

5. In a certain camera, a combination of four similar thin convex lenses are arranged axially in contact. Then the power of the combination and the total magnification in comparison to the power ( $p$ ) and magnification ( $m$ ) for each lens will be, respectively

- (1)  $p^4$  and  $m^4$                       (2)  $4p$  and  $4m$                       (3)  $p^4$  and  $4m$                       (4)  $4p$  and  $m^4$

Ans. (4)  $4p$  and  $m^4$

Sol.  $P_{eq} = P_1 + P_2 + P_3 + P_4 = 4P$   
 $m_{eq} = m_1 \cdot m_2 \cdot m_3 \cdot m_4 = m^4$

6. A 2 amp current is flowing through two different small circular copper coils having radii ratio 1 : 2. The ratio of their respective magnetic moments will be :

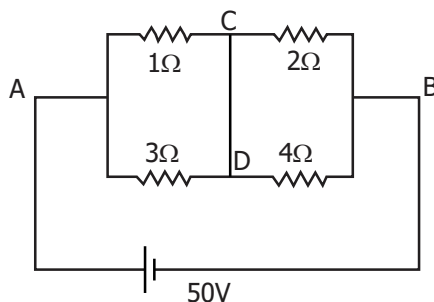
- (1) 4 : 1                      (2) 1 : 4                      (3) 1 : 2                      (4) 2 : 1

Ans. (2) 1 : 4

Sol.  $\mu = i\pi r^2$

$$\frac{\mu_1}{\mu_2} = \frac{1}{4}$$

7. A constant voltage of 50 V is maintained between the points A and B of the circuit shown in the figure. The current through the branch CD of the circuit is :



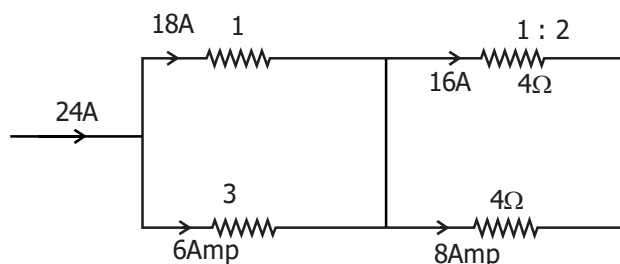
- (1) 3.0 A                      (2) 1.5 A                      (3) 2.0 A                      (4) 2.5 A



**Ans. (3) 2.0 A**

**Sol.**  $R_{eq} = \frac{3}{4} + \frac{4}{3} = \frac{25}{12}$

$$i = \frac{50}{25} \times 12 = 24 \text{ Amp}$$



So, difference of current will flow from  $i = 2$  Amp.

- 8.** Two gases A and B are filled at the same pressure in separate cylinders with movable pistons of radius  $r_A$  and  $r_B$ , respectively. On supplying an equal amount of heat to both the systems reversibly under constant pressure, the pistons of gas A and B are displaced by 16 cm and 9 cm, respectively. If the change in their internal energy is the same, then the ratio  $r_A/r_B$  is equal to :

- (1)  $\frac{\sqrt{3}}{2}$       (2)  $\frac{4}{3}$       (3)  $\frac{3}{4}$       (4)  $\frac{2}{\sqrt{3}}$

**Ans. (3)  $\frac{3}{4}$**

**Sol.**  $W_A = W_B$   
 $P \cdot \pi r_A^2 \cdot 16 = P \pi r_B^2 \cdot 9$

$$\frac{r_A^2}{r_B^2} = \frac{9}{16} \Rightarrow \frac{r_A}{r_B} = \frac{3}{4}$$

- 9.** A container has two chambers of volumes  $V_1 = 2$  litres and  $V_2 = 3$  litres separated by a partition made of a thermal insulator. The chambers contains  $n_1 = 5$  and  $n_2 = 4$  moles of ideal gas at pressures  $p_1 = 1$  atm and  $p_2 = 2$  atm, respectively. When the partition is removed, the mixture attains an equilibrium pressure of :

- (1) 1.8 atm      (2) 1.3 atm      (3) 1.6 atm      (4) 1.4 atm

**Ans. (3) 1.6 atm**

**Sol.**  $n_{eq} = n_1 + n_2$   
 $P_{eq} \cdot V_{eq} = P_1 V_1 + P_2 V_2$   
 $P_{eq} \times 5 = 1 \times 2 + 2 \times 3$   
 $P_{eq} = \frac{8}{5} = 1.6 \text{ atm}$



- 10.** The radius of Martian orbit around the Sun is about 4 times the radius of the orbit of Mercury. The Martian year is 687 Earth days. Then which of the following is the length of 1 year on Mercury :
- (1) 124 earth days      (2) 88 earth days      (3) 225 earth days      (4) 172 earth days

**Ans. (2) 88 earth days**

**Sol.** 
$$\frac{T_{\text{mass}}}{T_B} = \left( \frac{r_M}{r_B} \right)^{3/2}$$

$$\frac{687}{T_B} = 8 \Rightarrow T_B = \frac{687}{8} = 88 \text{ earth days}$$

- 11.** To an ac power supply of 220 V at 50 Hz, a resistor of  $20 \Omega$ , a capacitor of reactance  $25 \Omega$  and an inductor of reactance  $45 \Omega$  are connected in series. The corresponding current in the circuit and the phase angle between the current and the voltage is, respectively ;
- (1) 15.6 A and  $45^\circ$       (2) 7.8 A and  $30^\circ$       (3) 7.8 A and  $45^\circ$       (4) 15.6 A and  $30^\circ$

**Ans. (3) 7.8 A and  $45^\circ$**

**Sol.** 
$$Z = \sqrt{(X_L - X_C)^2 + R^2} = \sqrt{20^2 + (45 - 25)^2} = 20\sqrt{2}$$

$$i = \frac{220}{20\sqrt{2}} = \frac{11}{\sqrt{2}} = 7.8 \text{ Amp}$$

$$\tan \phi = \frac{X_L - X_C}{R} = \frac{20}{20} = 1$$

$$\phi = 45^\circ$$

- 12.** A wire of resistance R is cut into 8 equal pieces. From these pieces two equivalent resistances are made by adding four of these together in parallel. Then these two sets are added in series. The net effective resistance of the combination is :

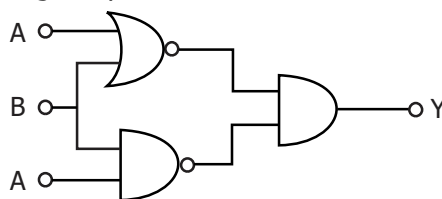
- (1)  $\frac{R}{8}$       (2)  $\frac{R}{64}$       (3)  $\frac{R}{32}$       (4)  $\frac{R}{16}$

**Ans. (4)  $\frac{R}{16}$**

**Sol.** Resistance of each wire =  $\frac{R}{8}$

$$R_{\text{eq}} = \frac{R}{8 \times 4} + \frac{R}{8 \times 4} = \frac{R}{16}$$

- 13.** The output (Y) of the given logic implementation is similar to the output of an/a ..... gate :



- (1) NOR      (2) AND      (3) NAND      (4) OR



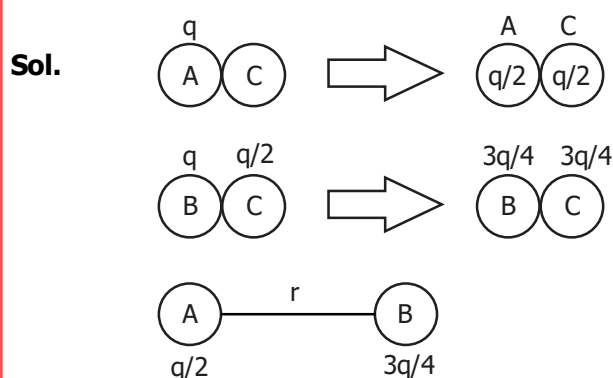
**Ans. (1) NOR**

**Sol.** 
$$y = (\overline{A+B}) \cdot (\overline{A \cdot B})$$
$$= (\overline{A} \cdot \overline{B}) \cdot (\overline{A} + \overline{B}) = \overline{A} \cdot \overline{A} \cdot \overline{B} + \overline{A} \cdot \overline{B} \cdot \overline{B}$$
$$= \overline{A} \cdot \overline{B} \text{ (NOR gate)}$$

**14.** Two identical charged conducting spheres A and B have their centres separated by a certain distance. Charge on each sphere is  $q$  and the force of repulsion between them is  $F$ . A third identical uncharged conducting sphere is brought in contact with sphere A first and then with B and finally removed from both. New force of repulsion between spheres A and B (Radii of A and B are negligible compared to the distance of separation so that for calculating force between them they can be considered as point charges) is best given as :

- (1)  $\frac{3F}{8}$                       (2)  $\frac{3F}{5}$                       (3)  $\frac{2F}{3}$                       (4)  $\frac{F}{2}$

**Ans. (1)  $\frac{3F}{8}$**



$$F_{\text{Pre}} = \frac{kq^2}{r^2} ; F' = \frac{K \cdot \frac{q}{2} \times \frac{3q}{4}}{r^2}$$

$$F' = \frac{3}{8} F$$

**15.** Consider the diameter of a spherical object being measured with the help of a Vernier callipers. Suppose its 10 Vernier Scale Divisions (V.S.D.) are equal to its 9 Main Scale Divisions (M.S.D.). The least division in the M.S. is 0.1 cm and the zero of V.S. is at  $x = 0.1$  cm when the jaws of Vernier callipers are Closed. If the main scale reading for the diameter is  $M = 5$  cm and the number of coinciding vernier division is 8, the measured diameter after zero error correction, is :

- (1) 5.00 cm                      (2) 5.18 cm                      (3) 5.08 cm                      (4) 4.98 cm

**Ans. (4) 4.98 cm**

**Sol.**  $9 \times \text{MSD} = 10 \text{ VSD}$

$$\text{VSD} = .9 \times \text{MSD}$$

$$\text{Least count} = \text{MSD} - .9 \text{ MSD}$$

$$= .01 \text{ cm}$$

$$R = 5 + (8 \times .01) - 1 \text{ [+ve zero error]}$$

$$= 5.08 - 1 = 4.98 \text{ cm}$$



16. In some appropriate units, time (t) and position (x) relation of a moving particle is given by  $t = x^2 + x$ . The acceleration of the particle is :

(1)  $+\frac{2}{2x+1}$       (2)  $-\frac{2}{(x+2)^3}$       (3)  $-\frac{2}{(2x+1)^3}$       (4)  $+\frac{2}{(x+1)^3}$

Ans. (3)  $-\frac{2}{(2x+1)^3}$

Sol.  $t = x^2 + x$

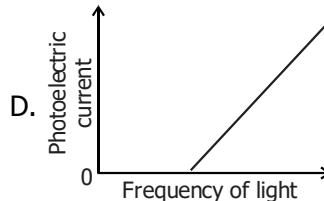
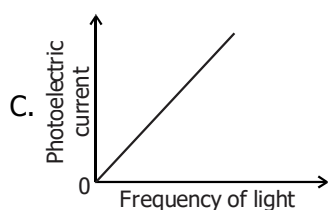
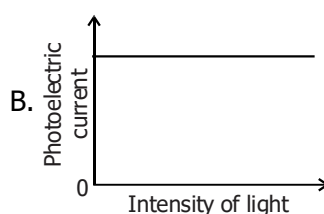
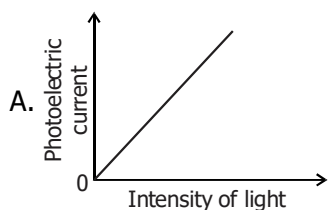
$$\frac{dt}{dx} = (2x+1)$$

$$\frac{dx}{dt} = v = (2x+1)^{-1}$$

$$\frac{dv}{dx} = -1(2x+1)^{-2} \times 2$$

$$a = v \cdot \frac{dv}{dx} = -(2x+1)^{-1} (2x+1)^{-2} = \frac{-2}{(2x+1)^3}$$

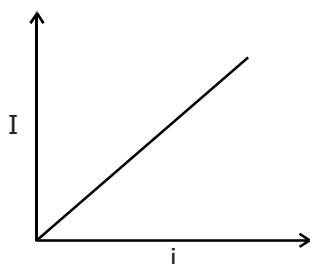
17. Which of the following options represent the variation of photoelectric current with property of light shown on the x-axis :



- (1) B and D      (2) A only      (3) A and C      (4) A and D

Ans. (2) A only

Sol. Photocurrent  $\propto$  Intensity





- 18.** A particle of mass  $m$  is moving around the origin with a constant force  $F$  pulling it towards the origin. If Bohr model is used to describe its motion, the radius  $r$  of the  $n^{\text{th}}$  orbit and the particle's speed  $v$  in the orbit depend on  $n$  as :

(1)  $r \propto n^{4/3}$  ;  $v \propto n^{-1/3}$  (2)  $r \propto n^{1/3}$  ;  $v \propto n^{1/3}$  (3)  $r \propto n^{1/3}$  ;  $v \propto n^{2/3}$  (4)  $r \propto n^{2/3}$  ;  $v \propto n^{1/3}$

**Ans. (4)  $r \propto n^{2/3}$  ;  $v \propto n^{1/3}$**

**Sol.**  $F = \frac{mv^2}{r}$  ;  $mvr = \frac{nh}{2\pi}$

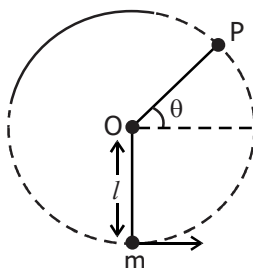
$v^2 \propto r$  ..... (1)

$vr \propto n$

$v \propto \frac{n}{r}$  ;  $\frac{n^2}{r^2} \propto r$

$r^3 \propto n^2$  ;  $r \propto n^{2/3}$  ;  $v \propto n^{1/3}$

- 19.** A bob of heavy mass  $m$  is suspended by a light string of length  $l$ . The bob is given a horizontal velocity  $v_0$  as shown in figure. If the string gets slack at some point P making an angle  $\theta$  from the horizontal, the ratio of the speed  $v$  of the bob at point P to its initial speed  $v_0$  is :



(1)  $\left(\frac{\sin \theta}{2+3 \sin \theta}\right)^{1/2}$  (2)  $(\sin \theta)^{1/2}$  (3)  $\left(\frac{1}{2+3 \sin \theta}\right)^{1/2}$  (4)  $\left(\frac{\cos \theta}{2+3 \sin \theta}\right)^{1/2}$

**Ans. (1)  $\left(\frac{\sin \theta}{2+3 \sin \theta}\right)^{1/2}$**

**Sol.**  $\frac{mv^2}{l} = mg \sin \theta$   
 $v^2 = l g \sin \theta$

Now By energy conservation

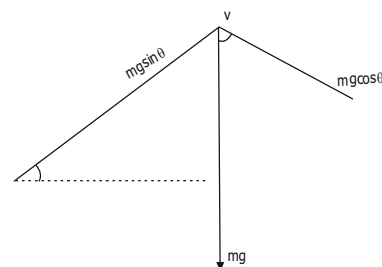
$K_i + U_i = K_f + U_f$

$\frac{1}{2}mv_0^2 = \frac{1}{2}m l g \sin \theta + mg(l + l \sin \theta)$

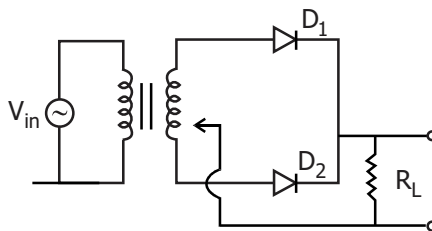
$V_0^2 = l g \sin \theta + 2gl + 2gl \sin \theta$

$V_0^2 = 2gl + 3gl \sin \theta$

$\frac{V}{V_0} = \left(\frac{\sin \theta}{2+3 \sin \theta}\right)^{1/2}$



- 20.** A full wave rectifier circuit with diodes ( $D_1$ ) and ( $D_2$ ) is shown in the figure. If input supply voltage  $V_{in} = 220\sin(100\pi t)$  volt, then at  $t = 15$  msec :



- (1)  $D_1$  and  $D_2$  both are reverse biased      (2)  $D_1$  is forward biased,  $D_2$  is reverse biased  
(3)  $D_1$  is reverse biased,  $D_2$  is forward biased      (4)  $D_1$  and  $D_2$  both are forward biased

**Ans. (3)  $D_1$  is reverse biased,  $D_2$  is forward biased**

**Sol.** at  $t = 15$  ms

$$V = 220 \sin(100\pi \times 1.5 \times 10^{-3}) \text{ (-ve)}$$

So diode  $D_1$  will be reverse and will be forward.

- 21.** A balloon is made of a material of surface tension  $S$  and its inflation outlet (from where gas is filled in it) has small area  $A$ . It is filled with a gas of density  $\rho$  and takes a spherical shape of radius  $R$ . When the gas is allowed to flow freely out of it, its radius  $r$  changes from  $R$  to 0 (zero) in time  $T$ . If the speed  $v(r)$  of gas coming out of the balloon depends on  $r$  as  $r^a$  and  $T \propto S^\alpha A^\beta \rho^\gamma R^\delta$  then :

- (1)  $a = \frac{1}{2}, \alpha = \frac{1}{2}, \beta = -\frac{1}{2}, \gamma = \frac{1}{2}, \delta = \frac{7}{2}$       (2)  $a = \frac{1}{2}, \alpha = \frac{1}{2}, \beta = -1, \gamma = 1, \delta = \frac{3}{2}$   
(3)  $a = -\frac{1}{2}, \alpha = -\frac{1}{2}, \beta = -1, \gamma = -\frac{1}{2}, \delta = \frac{5}{2}$       (4)  $a = -\frac{1}{2}, \alpha = -\frac{1}{2}, \beta = -1, \gamma = \frac{1}{2}, \delta = \frac{7}{2}$

**Ans. (4)  $a = -\frac{1}{2}, \alpha = -\frac{1}{2}, \beta = -1, \gamma = \frac{1}{2}, \delta = \frac{7}{2}$**

**Sol.**  $T \propto S^\alpha A^\beta \rho^\gamma R^\delta$

$$(m^0 L^0 T^1) \propto (M^1 L^0 T^{-2})^\alpha (L^2)^\beta (M L^{-3})^\gamma (L^1)^\delta$$

$$\alpha + \gamma = 0$$

$$2\alpha = 1$$

$$r = 1/2$$

$$\alpha = -1/2$$

matches with only 4 option

- 22.** A microscope has an objective of focal length 2 cm, eyepiece of focal length 4 cm and the tube length of 40 cm. If the distance of distinct vision of eye is 25 cm, the magnification in the microscope is :

- (1) 250      (2) 100      (3) 125      (4) 150

**Ans. (3) 125**

**Sol.**  $m = \frac{V_0}{u_0} \times \frac{D}{f_e}$

$$= \frac{L}{f_0} \times \frac{D}{f_e} = \frac{40}{2} \times \frac{24}{4} = 125$$





- 23.** Two identical point masses P and Q, suspended from two separate massless springs of spring constants  $k_1$  and  $k_2$ , respectively, oscillate vertically. If their maximum speeds are the same, the ratio ( $A_Q/A_P$ ) of the amplitude of  $A_Q$  of mass Q to the amplitude  $A_P$  of mass P is :

- (1)  $\sqrt{\frac{k_1}{k_2}}$       (2)  $\frac{k_2}{k_1}$       (3)  $\frac{k_1}{k_2}$       (4)  $\sqrt{\frac{k_2}{k_1}}$

**Ans.** (1)  $\sqrt{\frac{k_1}{k_2}}$

**Sol.**  $\sqrt{\frac{k_1}{k_2}}$

$$V_P = V_Q$$

$$A\omega = \text{constant} \quad A \propto \frac{1}{\omega} \propto \sqrt{\frac{m}{k}}$$

$$\frac{A_Q}{A_P} = \sqrt{\frac{k_1}{k_2}}$$

- 24.** A parallel plate capacitor made of circular plates is being charged such that the surface charge density on its plates is increasing at a constant rate with time. The magnetic field arising due to displacement current is :

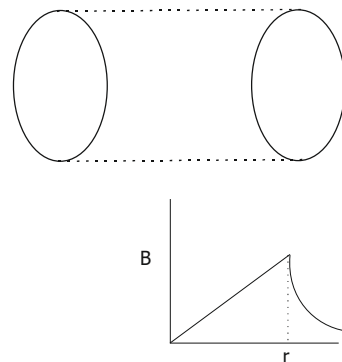
- (1) zero between the plates and non-zero outside  
(2) zero at all places  
(3) constant between the plates and zero outside the plates  
(4) non-zero everywhere with maximum at the imaginary cylindrical surface connecting peripheries of the plates

**Ans.** (4) non-zero everywhere with maximum at the imaginary cylindrical surface connecting peripheries of the plates

**Sol.**  $i = \epsilon_0 \frac{d\sigma}{dt} A$        $i$  constant

$i$  is constant But will be in cylindrical

so hypothetical cylindrical surface B is maximum





**25.** An electric dipole with dipole moment  $5 \times 10^{-6}$  Cm is aligned with the direction of a uniform electric field of magnitude  $4 \times 10^5$  N/C. The dipole is then rotated through an angle of  $60^\circ$  with respect to the electric field. The change in the potential energy of the dipole is :

- (1) 1.5 J                      (2) 0.8 J                      (3) 1.0 J                      (4) 1.2 J

**Ans. (3) 1.0 J**

**Sol.**  $\Delta U = PE(\cos\theta_1 - \cos\theta_2)$   
 $= 5 \times 10^{-6} \times 4 \times 10^5 (1 - \frac{1}{2})$   
 $= 5 \times 10^{-6} \times 4 \times \frac{1}{2} \times 10^5$   
 $= 1 \text{ Joule}$

**26.** There are two inclined surfaces of equal length (L) and same angle of inclination  $45^\circ$  with the horizontal. One of them is rough and the other is perfectly smooth. A given body takes 2 times as much time to slide down on rough surface than on the smooth surface. The coefficient of kinetic friction ( $\mu_k$ ) between the object and rough surface is close to :

- (1) 0.75                      (2) 0.25                      (3) 0.40                      (4) 0.5

**Ans. (1) 0.75**

**Sol.**  $t_1 = \sqrt{\frac{2h}{g \sin \theta}}$        $t_2 = \sqrt{\frac{2h}{(g \sin \theta - \mu g \cos \theta)}}$   
 $t_2 = 2t_1$   
 $\frac{1}{(\sin \theta - \mu \cos \theta)} = \frac{4}{\sin \theta}$   
 $\frac{1}{1 - \mu} = 4$        $1 - \mu = \frac{1}{4}$

**27.** De-Broglie wavelength of an electron orbiting in the  $n = 2$  state of hydrogen atom is close to :  
 (Given Bohr radius = 0.052 nm)

- (1) 2.67 nm                      (2) 0.067 nm                      (3) 0.67 nm                      (4) 1.67 nm

**Ans. (3) 0.67 nm**

**Sol.**  $2\pi r = n\lambda$   
 $2\pi r = 2\lambda$   
 $\lambda = \pi \times .052 \times 2^2 = .67 \text{ nm.}$

**28.** The Sun rotates around its centre once in 27 days. What will be the period of revolution if the Sun were to expand to twice its present radius without any external influence. Assume the Sun to be a sphere of uniform density :

- (1) 108 days                      (2) 100 days                      (3) 105 days                      (4) 115 days

**Ans. (1) 108 days**

**Sol.**  $L = I\omega = \text{constant}$   
 $MR^2 \frac{2\pi}{T_1} = M.4R^2 \frac{2\pi}{T_2}$   
 $T_2 = 4T_1 = 4 \times 27 = 108 \text{ days}$



- 29.** A physical quantity P is related to four observations a, b, c and d as follows :  $P = a^3 b^2 / c \sqrt{d}$   
The percentage errors of measurement in a, b, c and d are 1%, 3%, 2% and 4% respectively. The percentage error in the quantity P is :

(1) 15% (2) 10% (3) 2% (4) 13%

**Ans. (4) 13%**

**Sol.** 
$$\frac{\Delta P}{P} = 3 \frac{\Delta a}{a} + 2 \frac{\Delta b}{b} + \frac{\Delta c}{c} + \frac{1}{2} \times \frac{\Delta d}{d}$$
$$= 3 \times 1\% + 2 \times 3\% + 0 \times 2\% + \frac{1}{2} \times 4\%$$
$$3 + 6 + 2 + 2 = 13\%$$

- 30.** The plates of a parallel plate capacitor are separated by d. Two slabs of different dielectric constant  $K_1$  and  $K_2$  with thickness  $\frac{3}{8}d$  and  $\frac{d}{2}$ , respectively are inserted in the capacitor. Due to this, the capacitance becomes two times larger than when there is nothing between the plates. If  $K_1 = 1.25 K_2$ , the value of  $K_1$  is :

(1) 1.33 (2) 2.66 (3) 2.33 (4) 1.60

**Ans. (2) 2.66**

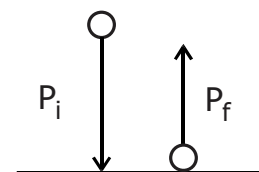
**Sol.** 
$$C' = 2C_0$$
$$\frac{A\epsilon_0}{d - \left(\frac{3d}{8} + \frac{d}{2}\right) + \left(\frac{3d}{8K_1} + \frac{d \times 5}{2 \times 4K_1}\right)} = \frac{2A\epsilon_0}{d}$$
$$\frac{1}{1 - \frac{7}{8} + \frac{1}{K_1}} = 2$$
$$\frac{1}{\frac{1}{8} - \frac{1}{K_1}} = 2 \Rightarrow 1 = \frac{1}{4} - \frac{2}{K_1}$$
$$K_1 = \frac{8}{3} = 2.66$$

- 31.** A ball of mass 0.5 kg is dropped from a height of 40 m. The ball hits the ground and rises to a height of 10 m. The impulse imparted to the ball during its collision with the ground is : (Take  $g = 9.8 \text{ m/s}^2$ )

(1) 84 NS (2) 21 NS (3) 7 NS (4) 0

**Ans. (2) 21 NS**

**Sol.** Impulse  $\Delta P = m[\sqrt{2gh_2} + \sqrt{2gh_1}]$ 
$$= \frac{1}{2} [\sqrt{800} + \sqrt{2 \times 10 \times 10}]$$
$$= \frac{10}{2} [\sqrt{8} + \sqrt{2}] = 21 \text{ NS}$$





- 32.** Two cities X and Y are connected by a regular bus service with a bus leaving in either direction every T min. A girl is driving scooter with a speed of 60 km/h in the direction X to Y notices that a bus goes past her every 30 minutes in the direction of her motion, and every 10 minutes in the opposite period T of the bus service and the speed (assumed constant) of the buses :

(1) 15 min, 120 km/h (2) 9 min, 40 km/h (3) 25 min, 100 km/h (4) 10 min, 90 km/h

**Ans. (1) 15 min, 120 km/h**

**Sol.** Distance between two buses

$$v_{\text{girl}} = \frac{60 \text{ km}}{60 \text{ min}}$$

$$= 1 \text{ km/min}$$

$$30 = \frac{VT}{1 - V} \quad \dots\dots\dots (1)$$

$$10 = \frac{VT}{1 + V} \quad \dots\dots\dots (2)$$

$$30 - 3V = 10 + 10 V$$

$$20 = 40 V$$

$$V = 2 \text{ km/min or } 120 \text{ km/h}$$

$$30 = \frac{2T}{1 - V}$$

$$10 = \frac{2T}{3}$$

$$T = 15 \text{ min}$$

- 33.** An oxygen cylinder of volume 30 litre has 18.20 moles of oxygen. After some oxygen is withdrawn from the cylinder, its gauge pressure drops to 11 atmospheric pressure at temperature 27°C. The mass of the oxygen withdrawn from the cylinder is nearly equal to :

[Given,  $R = \frac{100}{12} \text{ Jmol}^{-1}\text{K}^{-1}$ , and molecular mass of  $\text{O}_2 = 32$ , 1 atm pressure =  $1.01 \times 10^5 \text{ N/m}^2$ ]

(1) 0.156 kg (2) 0.125 kg (3) 0.144 kg (4) 0.116 kg

**Ans. (4) 0.116 kg**

**Sol.** Mass in container

$$m_1 = 18.20 \text{ mole} \times 32 \text{ gm} = 582.4 \text{ gm}$$

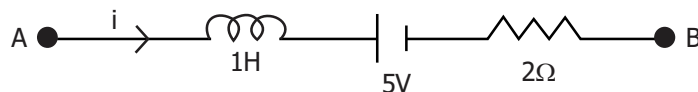
$$PV = \frac{m'}{M_0} RT$$

$$12 \times 1.01 \times 10^5 \times 30 \times 10^{-3} = \frac{m'}{32} \times \frac{100}{12} \times 300$$

$$m' = 465.4 \text{ gm}$$

$$\Delta m = m_1 - m' = 582.4 - 465.4 = 116 \text{ gm} = 0.116 \text{ kg}.$$

- 34.** AB is a part of an electrical circuit (see figure). The potential difference " $V_A - V_B$ ", at the instant when current  $i = 2A$  and is increasing at a rate of 1 amp/second is :



- (1) 10 volt                      (2) 5 volt                      (3) 6 volt                      (4) 9 volt

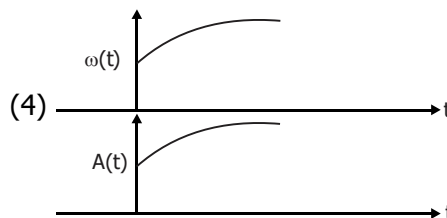
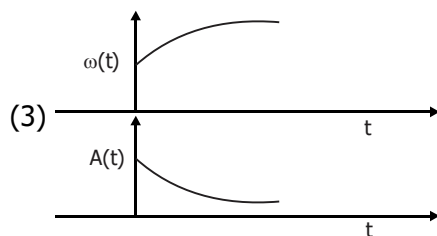
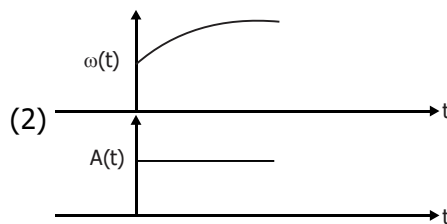
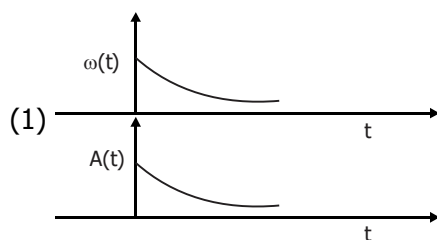
**Ans. (1) 10 volt**

**Sol.**  $V_A - L \times \frac{di}{dt} - 5 - ir - V_B = 0$

$$V_A - 1 - 5 - 4 - V_B = 0$$

$$V_A - V_B = 10 \text{ volt}$$

- 35.** In an oscillating spring mass system, a spring is connected to a box filled with sand. As the box oscillates, sand leaks slowly out of the box vertically so that the average frequency  $\omega(t)$  and average amplitude  $A(t)$  of the system change with time  $t$ . Which one of the following options schematically depicts these changes correctly :



**Ans. (2)**

**Sol.** amp do not depends on mass.

$$w = \sqrt{\frac{K}{m}}$$

- 36.** A model for quantized motion of an electron in a uniform magnetic field  $B$  states that the flux passing through the orbit of the electron is  $n(h/e)$  where  $n$  is an integer,  $h$  is Planck 's constant and  $e$  is the magnitude of electron's charge. According to the model, the magnetic moment of an electron in its lowest energy state will be : ( $m$  is the mass of the electron)

- (1)  $\frac{heB}{2\pi m}$                       (2)  $\frac{he}{\pi m}$                       (3)  $\frac{he}{2\pi m}$                       (4)  $\frac{heB}{\pi m}$

**Ans. (3)  $\frac{he}{2\pi m}$**



**Sol.**  $B \cdot \pi r^2 = \frac{h}{e} \{ n = 1 \}$

$$r = \sqrt{\frac{h}{eB\pi}} \dots (1)$$

$$e \times B = \frac{mv}{r} \quad v = \frac{eBr}{m}$$

$$\mu = \frac{eVr}{2} = \frac{e}{2} \cdot \frac{eB}{m} \cdot r^2$$

$$e^2 \frac{B}{m} \cdot \frac{h}{eB\pi} = \frac{he}{2\pi m}$$

**37.** A body weighs 48 N on the surface of the earth. The gravitational force experienced by the body due to the earth at a height equal to one-third the radius of the earth from its surface is :

- (1) 36 N                      (2) 16 N                      (3) 27 N                      (4) 32 N

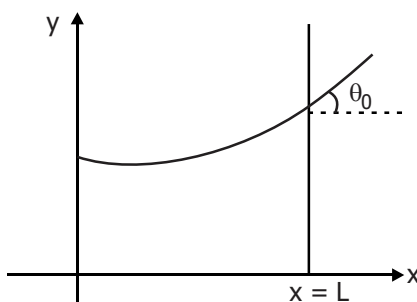
**Ans. (3) 27 N**

**Sol.**  $mg = 48 \Rightarrow m = \frac{48}{g}$

$$w = \frac{48}{g} \times g_h = \frac{48}{g} \times \frac{gR^2}{(R+h)^2}$$

$$= 48 \times \frac{R^2}{\left(R^2 + \frac{R}{3}\right)^2} = 48 \times \frac{R^2 \times g}{16R^2} = 3 \times 9 = 27N$$

**38.** Consider a waiter tank shown in the figure. It has one wall at  $x = L$  and can be taken to be very wide in the  $z$  direction. When filled with a liquid of surface tension  $S$  and density  $\rho$ , the liquid surface makes angle  $\theta_0$  ( $\theta_0 < 1$ ) with the  $x$ -axis at  $x = L$ . If  $y(x)$  is the height of the surface then the equation for  $y(x)$  is :



(take  $\theta(x) = \sin\theta(x) = \tan\theta(x) = \frac{dy}{dx}$ ,  $g$  is the acceleration due to gravity)

- (1)  $\frac{dy}{dx} = \sqrt{\frac{\rho g}{S}} x$                       (2)  $\frac{d^2y}{dx^2} = \frac{\rho g}{S} x$                       (3)  $\frac{d^2y}{dx^2} = \frac{\rho g}{S} y$                       (4)  $\frac{d^2y}{dx^2} = \sqrt{\frac{\rho g}{S}}$

**Ans. (3)  $\frac{d^2y}{dx^2} = \frac{\rho g}{S} y$**



**Sol.** radius of curvatre  $r = \frac{d^2y / dx^2}{\left(1 + \frac{d^2y}{dx^2}\right)^{3/2}}$

By Using Laplace equation

$$\rho g y = r.s$$

$$\frac{\rho g \cdot y}{s} = \frac{d^2y}{dx^2}$$

**II-method :**

F = force due to surface tension

$$F = S \times Z \dots (1)$$

this force is balanced by weight of liq.

$$W = mg$$

$$W = \rho \times xyz \times g \dots (2)$$

$$\Delta \sin \theta = \rho xyz \times g$$

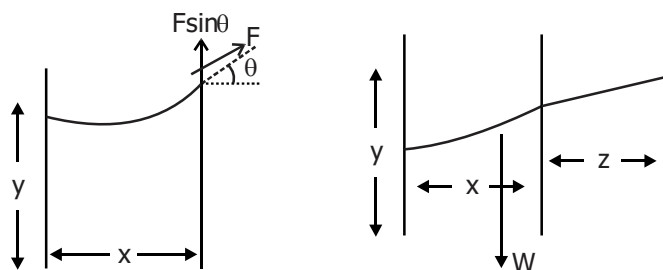
$$\sin \theta = \tan \theta$$

$$\delta \times \tan \theta = \rho xyz$$

$$\delta \times \frac{dy}{dx} = \rho xyz$$

$$\frac{dy}{dx} = \frac{\rho xyz}{s}$$

$$\frac{d^2y}{dx^2} = \frac{\rho g}{\delta} y$$



**39.** The intensity of transmitted light when a polaroid sheet, placed between two crossed polaroids at  $22.5^\circ$  from the polarization axis of one of the Polaroid, is :

( $I_0$  is the intensity of polarised light after passing through the first polaroid)

(1)  $\frac{I_0}{16}$

(2)  $\frac{I_0}{2}$

(3)  $\frac{I_0}{4}$

(4)  $\frac{I_0}{8}$

**Ans.** (4)  $\frac{I_0}{8}$

**Sol.** I from 1st polaroid is  $I_0$

$$I \text{ from 2 polaroid} = I_0 \cos^2 22.5^\circ$$

$$I \text{ from 3 polaroid} = I_0 \cos^2 (90^\circ - 22.5^\circ)$$

$$I = I_0 \sin^2 22.5^\circ \cdot \cos^2 22.5^\circ$$

$$= I_0 \frac{4}{4} \sin^2 22.5^\circ \cos^2 22.5^\circ$$

$$= \frac{I_0}{4} \times \sin^2 45^\circ = \frac{I_0}{8}$$



**40.** A photon and an electron (mass  $m$ ) have the same energy  $E$ . The ratio ( $\lambda_{\text{photon}}/\lambda_{\text{electron}}$ ) of their de Broglie wavelengths is : ( $c$  is the speed of light)

- (1)  $\frac{1}{c} \sqrt{\frac{E}{2m}}$       (2)  $\sqrt{\frac{E}{2m}}$       (3)  $c\sqrt{2mE}$       (4)  $c\sqrt{\frac{2m}{E}}$

**Ans.** (4)  $c\sqrt{\frac{2m}{E}}$

**Sol.**  $\lambda_{\text{photon}} = \frac{hc}{E}$ ,  $\lambda_{\text{electron}} = \frac{h}{\sqrt{2mE}}$

$$\frac{\lambda_{\text{electron}}}{\lambda_{\text{photon}}} = \frac{hc\sqrt{2mE}}{E \cdot h} = c \cdot \sqrt{\frac{2m}{E}}$$

**41.** An unpolarized light beam travelling in air is incident on a medium of refractive index 1.73 at Brewster's angle. Then :

- (1) transmitted light is completely polarized with angle of refraction close to  $30^\circ$   
(2) reflected light is completely polarized and the angle of reflection is close to  $60^\circ$   
(3) reflected light is partially polarized and the angle of reflection is close to  $30^\circ$   
(4) both reflected and transmitted light are perfectly polarized with angles of reflection and refraction close to  $60^\circ$  and  $30^\circ$ , respectively

**Ans.** (2) reflected light is completely polarized and the angle of reflection is close to  $60^\circ$ .

**Sol.**  $\mu = 1.75$  so By Brewster law.

$$\mu = \tan \theta_p$$

$$\sqrt{3} = \tan \theta_p$$

$$\theta_p = 60^\circ$$

Reflected Ray will perfectly polarized.

$$\frac{\sin i}{\sin r} = \mu$$

$$\frac{\sin 60^\circ}{\sin r} = \sqrt{3} \quad \sin r = \frac{1}{2} \quad \boxed{r = 30^\circ}$$

**42.** An uniform rod of mass 20 kg and length 5 m leans against a smooth vertical wall making an angle of  $60^\circ$  with it. The other end rests on a rough horizontal floor. The friction force that the floor exerts on the rod is : (take  $g = 10 \text{ m/s}^2$ )

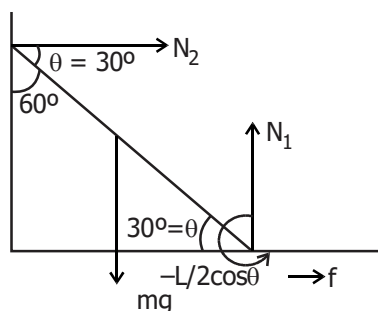
- (1)  $200\sqrt{3} \text{ N}$       (2)  $100 \text{ N}$       (3)  $100\sqrt{3} \text{ N}$       (4)  $200 \text{ N}$

**Ans.** (3)  $100\sqrt{3} \text{ N}$

**Sol.** Torque Balancing

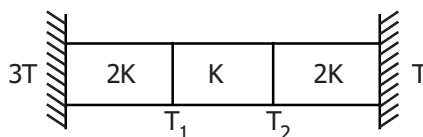
$$mg \times \frac{L}{2} \cos \theta = N_2 \times L \sin \theta$$





$$N_2 = \frac{mg}{\cot 60} L_2 = 200 \times \frac{1}{2} \times \sqrt{3}$$

- 43.** Three identical heat conducting rods are connected in series as shown in the figure. The rods on the sides have thermal conductivity  $2K$  while that in the middle has thermal conductivity  $K$ . The left end of the combination is maintained at temperature  $3T$  and the right end at  $T$ . The rods are thermally insulated from outside. In steady state, temperature at the left junction is  $T_1$  and that at the right-junction is  $T_2$ . The ratio  $T_1/T_2$  is :



- (1)  $\frac{5}{4}$                       (2)  $\frac{3}{2}$                       (3)  $\frac{4}{3}$                       (4)  $\frac{5}{3}$

**Ans.** (4)  $\frac{5}{3}$

**Sol.** Consider resistance

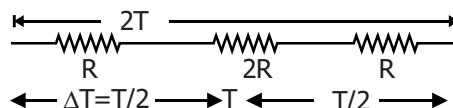
$$\Delta T_1 : \Delta T_2 : \Delta T_3$$

$$1 : 2 : 1$$

$$T_A = 3T - T / 2 = 5T / 2 \dots\dots (1)$$

$$T_B = \frac{5T}{2} - T = \frac{3T}{2}$$

$$\frac{T_A}{T_B} = \frac{5}{3}$$



$$\Delta T_1 : \Delta T_2 : \Delta T_3$$

$$1 : 2 : 1$$

- 44.** The kinetic energies of two similar cars A and B are 100 J and 225 J respectively. On applying breaks, car A stops after 1000 m and car B stops after 1500 m. If  $F_A$  and  $F_B$  are the forces applied by the breaks on cars A and B, respectively, then the ratio  $F_A/F_B$  is :

- (1)  $\frac{1}{2}$                       (2)  $\frac{3}{2}$                       (3)  $\frac{2}{3}$                       (4)  $\frac{1}{3}$

**Ans.** (3)  $\frac{2}{3}$

**Sol.** Work done by  $F = \Delta K$

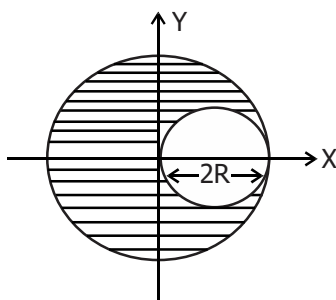
$$100 = F_A \cdot 1000 \quad \dots (1)$$

$$225 = F_B \cdot 1500 \quad \dots (2)$$

$$\frac{100}{225} = \frac{F_A}{F_B} \times \frac{2}{3}$$

$$\frac{F_A}{F_B} = \frac{2}{3}$$

- 45.** A sphere of radius  $R$  is cut from a larger solid sphere of radius  $2R$  as shown in the figure. The ratio of the moment of inertia of the smaller sphere to that of the rest part of the sphere about the  $Y$ -axis is :



(1)  $\frac{7}{64}$

(2)  $\frac{7}{8}$

(3)  $\frac{7}{40}$

(4)  $\frac{7}{57}$

**Ans.** (4)  $\frac{7}{57}$

**Sol.** 
$$M_{\text{cut part}} = \frac{4}{3} \pi (2R)^3 \times \frac{M}{8} = \frac{M}{8}$$

$$I_{\text{small}} = \frac{7}{5} \times \frac{M}{8} \times R^2 = \frac{7}{40} MR^2 \dots (1)$$

$$I_{\text{remain}} = \frac{2}{5} M \times 4R^2 - \frac{7}{40} MR^2$$

$$\frac{I_{\text{small}}}{I_{\text{remain}}} = \frac{7/40}{\left(\frac{8}{5} - \frac{7}{40}\right)} = \frac{7/40}{\frac{64-7}{40}} = \frac{7}{57}$$